



**中国科学院近代物理研究所**  
Institute of Modern Physics, Chinese Academy of Sciences

# **Neutral-Current Weak Interactions at an EIC**

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In collaborate with Krishna Kumar, Abhay Deshpande, Jin Huang, Seamus Riordan

# Outline

- Introduction of electroweak interactions in electron scatterings
- Electroweak physics study at an EIC
  - Nucleon spin structure
  - The weak mixing angle  $\sin^2\theta_w$
- Summary

# Discovery of Parity Violation

Symmetries play a central role in physics. Parity, Time Reversal, Charge Conjugation, ..., were naturally assumed to be conserved until

T.D. Lee and C.N. Yang first suggested parity violation. Awarded Nobel Prize 1957 after experimental confirmation.

"for their penetrating investigation of the so-called parity laws which has led to important discoveries regarding the elementary particles"

C. S. Wu led the experiment confirmed parity violation in nuclear  $\beta$ -decay

Glashow-Weinberg-Salam (GWS) theory yields the unification of electroweak interaction and predicts Z boson



Tsung-Dao Lee



Chen-Ning Yang



Chien-Shiung Wu

# Electro-weak interactions

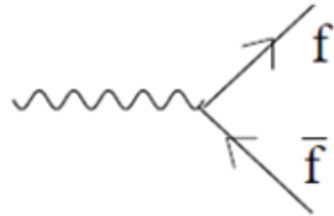
Spin-1/2 particles carry two types of couplings: Axial and Vector

**Axial:** difference of strength for left/right handed states

**Vector:** Average of the two

$\gamma$

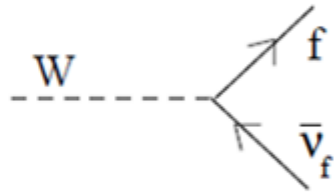
$$-iQ\gamma^\mu$$



No difference for left/right particle  
Vector coupling =  $Q$

$W^\pm$

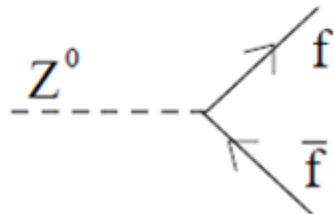
$$-i\frac{g}{\sqrt{2}}\gamma^\mu\frac{1}{2}(1-\gamma^5)$$



Only interact with left-handed fermions

$Z^0$

$$-i\frac{g}{\cos\theta_W}\gamma^\mu\frac{1}{2}(g_V^e - g_A^e\gamma^5)$$



Interact with both left and right handed fermions

$$g_A^e = -\frac{1}{2}$$

$$g_V^e = -\frac{1}{2} + 2\sin^2\theta_W = -0.036$$

# Parity Violating in Electron Scatterings

## --- Neutral current

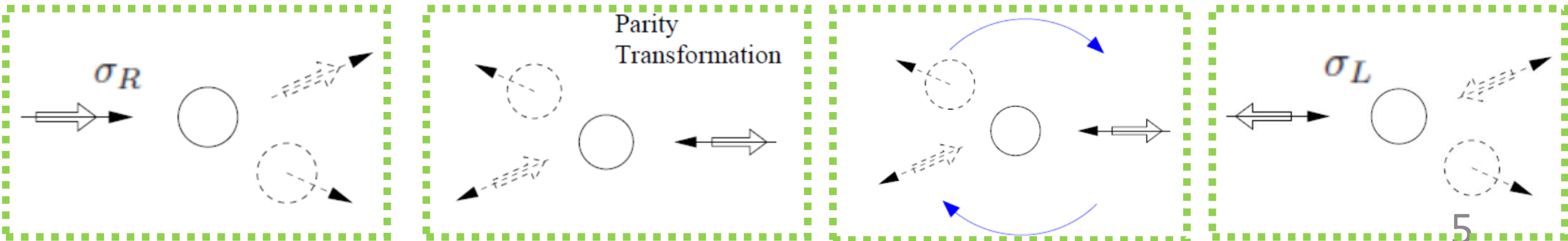
$$\sigma \sim \left| \begin{array}{c} \text{No PV} \\ \text{Yes PV} \end{array} \right|^2$$

$\gamma^*$   
 $e$   $e_q$   
 $g_V^e - g_A^e \gamma^5$

$Z^0$   
 $e$   $q$   
 $g_V^q - g_A^q \gamma^5$

*In context of SM  
Tree level...*

To detect PV : **long. pol. Electron + unpol. Nucl.**



# Parity Violating in Electron Scattering

## --- Neutral current

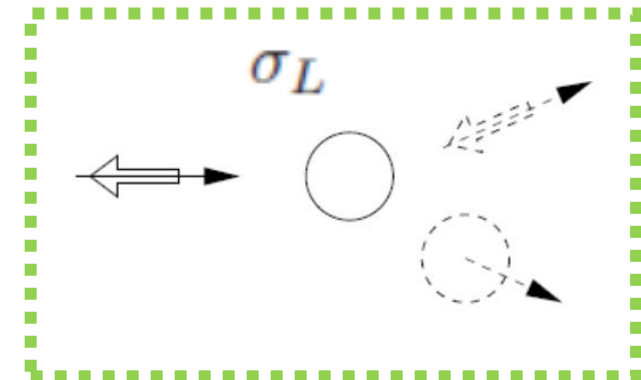
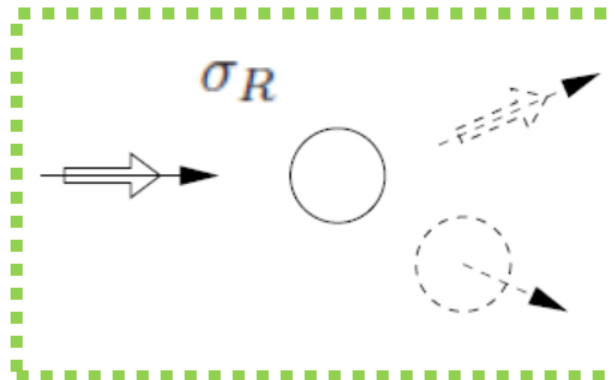
$$\sigma \sim \left| \begin{array}{c} \text{No PV} \\ \text{Yes PV} \end{array} \right|^2$$

$\gamma^*$   
 $e$   $e_q$   
 $g_V^e - g_A^e \gamma^5$   $g_V^q - g_A^q \gamma^5$

*In context of SM  
Tree level...*

To detect PV : **long. pol. Electron + unpol. Nucl.**

$$A_{PV} \equiv \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L}$$



# Flavor Decompositions

## --- an example for polarized case

- With pure  $\gamma$  exchange in inclusive DIS:

$$g_1^P = \frac{1}{2} \left( \frac{4}{9}(\Delta u + \Delta \bar{u}) + \frac{1}{9}(\Delta d + \Delta \bar{d}) + \frac{1}{9}(\Delta s + \Delta \bar{s}) \right)$$
$$g_1^n = \frac{1}{2} \left( \frac{1}{9}(\Delta u + \Delta \bar{u}) + \frac{4}{9}(\Delta d + \Delta \bar{d}) + \frac{1}{9}(\Delta s + \Delta \bar{s}) \right)$$

- **Assumption: SU(3) flavor symmetry**

- ✓ Additional inputs from  $\beta$ -decay of neutron and hyperons

$$\Delta u + \Delta d - 2 \Delta s$$

$$\Delta u + \Delta d$$

- ✓ SIDIS measurements also provide information with quark flavors, fragmentation functions provide different weights

Hmm ... No third kind  
of nucleon ... No...



**Electroweak interactions in DIS region at an EIC can have new inputs...**

# EIC offers new opportunities with weak neutral currents

Anselmino, Efremov, Leader, Ji ...

Phys. Rep. 216 (1995)

$$\frac{d^2\sigma_{nc}^{\ell N}}{d\Omega dE'} = \frac{1}{2m_N(4\pi)^2} \frac{E'}{E} \times |M_\gamma + M_Z|^2$$

$$\begin{aligned} \frac{d^2\sigma_{nc}^{\ell N}}{dx dy}(\lambda, S = S_L) = & 4\pi m_N E y \frac{\alpha^2}{Q^4} \sum_i \eta^i C^i \\ & \times \left\{ 2xy F_1^i + \frac{2}{y} \left( 1 - y - \frac{xy m_N}{2E} \right) (F_2^i + g_3^i) \right. \\ & - 2\lambda x \left( 1 - \frac{y}{2} \right) F_3^i - 2\lambda x \left( 2 - y - \frac{xy m_N}{E} \right) g_1^i \\ & + 4\lambda \frac{x^2 m_N}{E} g_2^i - \frac{2}{y} \left( 1 + \frac{xm_N}{E} \right) \left( 1 - y - \frac{xy m_N}{2E} \right) g_4^i \\ & \left. + 2xy \left( 1 + \frac{xm_N}{E} \right) g_5^i \right\}, \end{aligned}$$

**With parity violation and  $Q^2 \ll Z^2$**

**Inclusive electron measurements**

**pol. electron & unpol. nucleon:**

$$A_{beam} = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_A^e \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e \frac{Y_-}{2Y_+} \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$

**unpol. electron & pol. nucleon:**

$$A_L = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_V^e \frac{g_5^{\gamma Z}}{F_1^\gamma} + g_A^e \frac{Y_-}{Y_+} \frac{g_1^{\gamma Z}}{F_1^\gamma} \right]$$



# New structure functions

## --- $\gamma$ -Z interference structure functions

pol. electron & unpol. nucleon:

$$A_{beam} = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_A^e \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e \frac{Y_-}{2Y_+} \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$

$$F_1^{\gamma Z} = \sum_f e_{q_f} (g_V)_{q_f} (q_f + \bar{q}_f)$$

$$F_3^{\gamma Z} = 2 \sum_f e_{q_f} (g_A)_{q_f} (q_f - \bar{q}_f)$$

unpol. electron & pol. nucleon:

$$A_L = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_V^e \frac{g_5^{\gamma Z}}{F_1^\gamma} + g_A^e \frac{Y_-}{Y_+} \frac{g_1^{\gamma Z}}{F_1^\gamma} \right]$$

$$g_1^{\gamma Z} = \sum_f e_{q_f} (g_V)_{q_f} (\Delta q_f + \Delta \bar{q}_f)$$

$$g_5^{\gamma Z} = \sum_f e_{q_f} (g_A)_{q_f} (\Delta q_f - \Delta \bar{q}_f)$$

New and unique combinations of individual PDFs

# New structure functions

## --- $\gamma$ -Z interference structure functions

pol. electron & unpol. nucleon:

$$A_{beam} = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_A^e \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e \frac{Y_-}{2Y_+} \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$

$$F_1^{p, \gamma Z} \approx \frac{1}{9}(u + \bar{u} + d + \bar{d} + s + \bar{s} + c + \bar{c})$$

$$F_1^{n, \gamma Z} \approx \frac{1}{9}(u + \bar{u} + d + \bar{d} + s + \bar{s} + c + \bar{c})$$

$$F_3^{p, \gamma Z} = \frac{2}{3}(u_V + c - \bar{c}) + \frac{1}{3}(d_V + s - \bar{s})$$

$$F_3^{n, \gamma Z} = \frac{2}{3}(d_V + s - \bar{s}) + \frac{1}{3}(u_V + c - \bar{c})$$

unpol. electron & pol. nucleon:

$$A_L = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_V^e \frac{g_5^{\gamma Z}}{F_1^\gamma} + g_A^e \frac{Y_-}{Y_+} \frac{g_1^{\gamma Z}}{F_1^\gamma} \right]$$

$$g_1^{p, \gamma Z} \approx \frac{1}{9}(\Delta u + \Delta \bar{u} + \Delta d + \Delta \bar{d} + \Delta s + \Delta \bar{s} + \Delta c + \Delta \bar{c})$$

$$g_1^{n, \gamma Z} \approx \frac{1}{9}(\Delta u + \Delta \bar{u} + \Delta d + \Delta \bar{d} + \Delta s + \Delta \bar{s} + \Delta c + \Delta \bar{c})$$

$$g_5^{p, \gamma Z} = \frac{1}{3}(\Delta u_V + \Delta c - \Delta \bar{c}) + \frac{1}{6}(\Delta d_V + \Delta s - \Delta \bar{s})$$

$$g_5^{n, \gamma Z} = \frac{1}{3}(\Delta d_V + \Delta s - \Delta \bar{s}) + \frac{1}{6}(\Delta u_V + \Delta c - \Delta \bar{c})$$

# W exchange in DIS region

PHYSICAL REVIEW D **88**, 114025 (2013)

## Prospects for charged current deep-inelastic scattering off polarized nucleons at a future electron-ion collider

Elke C. Aschenauer,<sup>\*</sup> Thomas Burton,<sup>†</sup> and Marco Stratmann<sup>‡</sup>

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Till Martini<sup>§</sup>

*Institut für Physik, Humboldt-Universität zu Berlin, D-12489 Berlin, Germany*

Hubert Spiesberger<sup>||</sup>

*PRISMA Cluster of Excellence, Institut für Physik, Johannes Gutenberg-Universität,  
Staudingerweg 7, D-55099 Mainz, Germany*

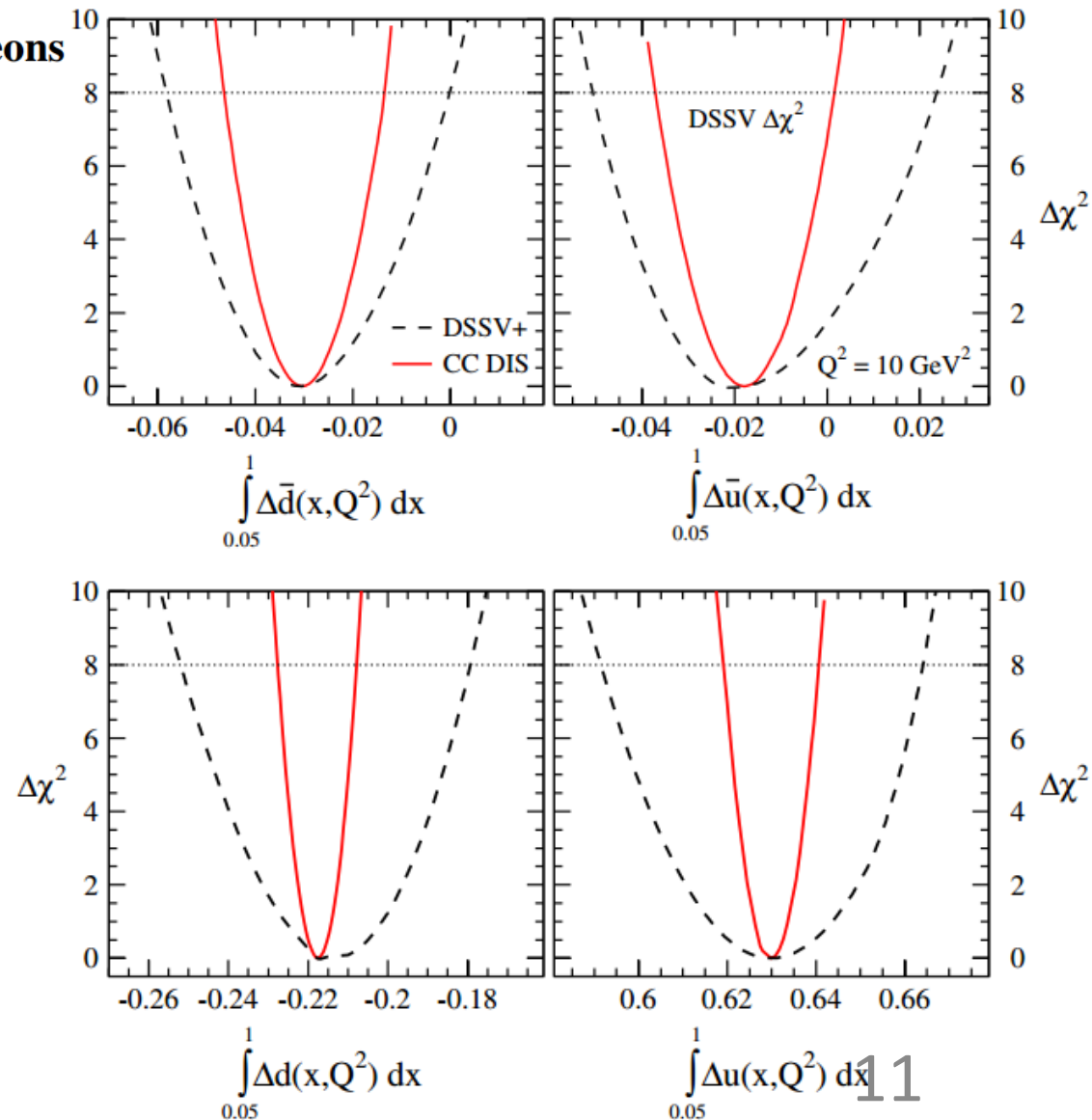
(Received 23 September 2013; published 9 December 2013)

$$g_1^{W^-,p}(x) = \Delta u(x) + \Delta \bar{d}(x) + \Delta c(x) + \Delta \bar{s}(x),$$

$$g_5^{W^-,p}(x) = -\Delta u(x) + \Delta \bar{d}(x) - \Delta c(x) + \Delta \bar{s}(x)$$

$$g_1^{W^+,p}(x) = \Delta \bar{u}(x) + \Delta d(x) + \Delta \bar{c}(x) + \Delta s(x),$$

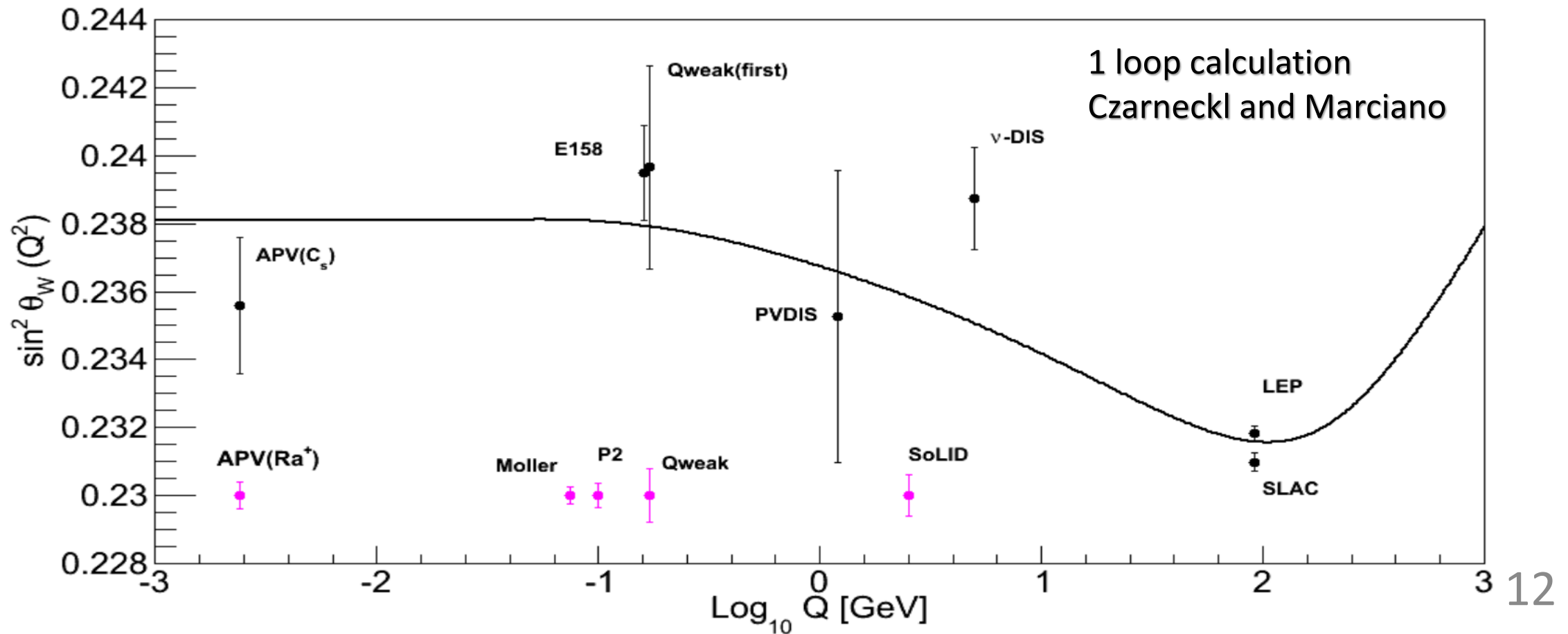
$$g_5^{W^+,p}(x) = \Delta \bar{u}(x) - \Delta d(x) + \Delta \bar{c}(x) - \Delta s(x)$$



# Parity-violating asymmetries in e-D collisions

- Deuteron has same amount of u and d in  $x > 0.2$  region
- $APV \sim 20/3 \sin^2 \theta_w - 1$
- Fundamental quantity in SM, constraints on new physics, such as new Z boson etc.

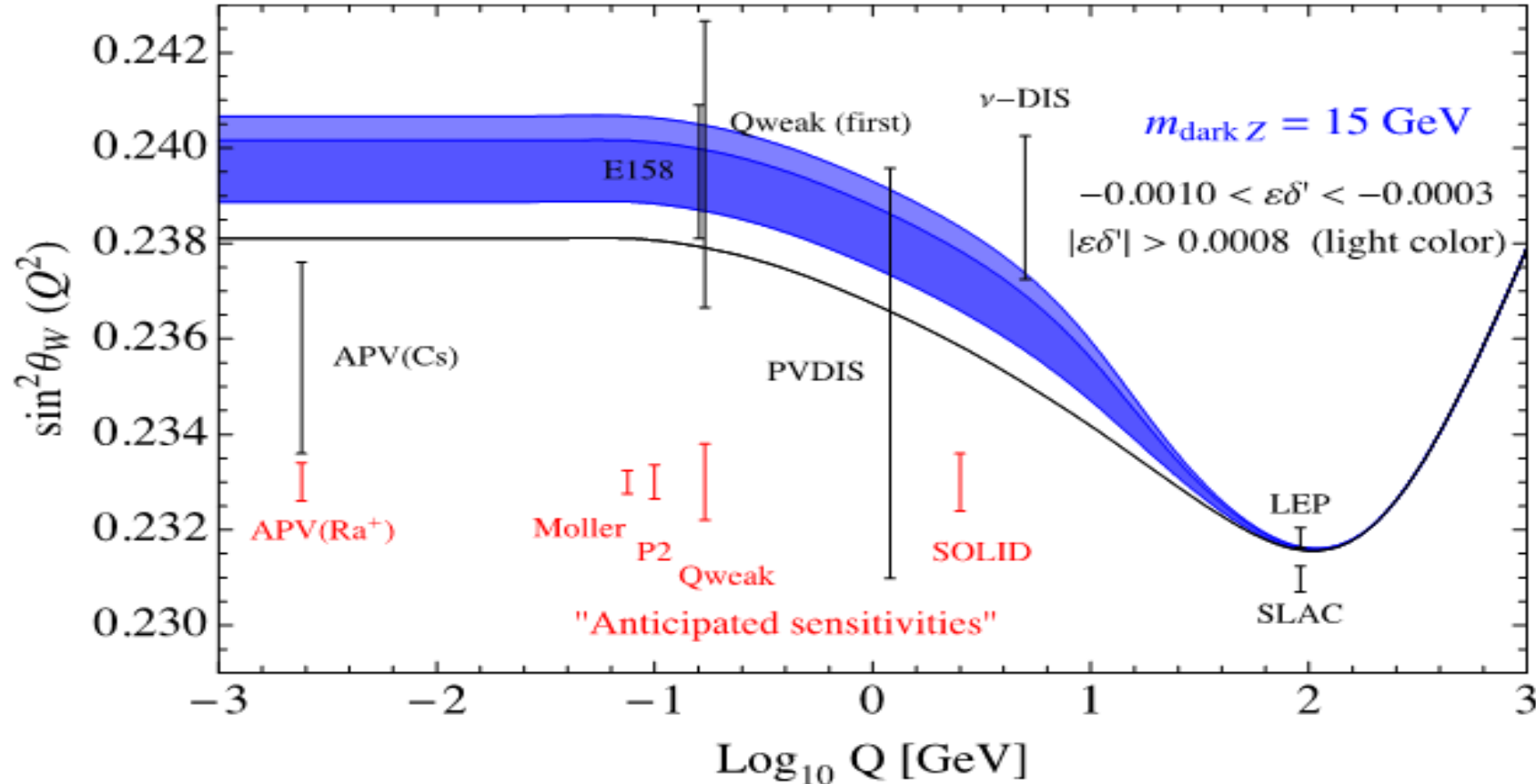
$$A_{beam} = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_A^e \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e \frac{Y_-}{2Y_+} \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$



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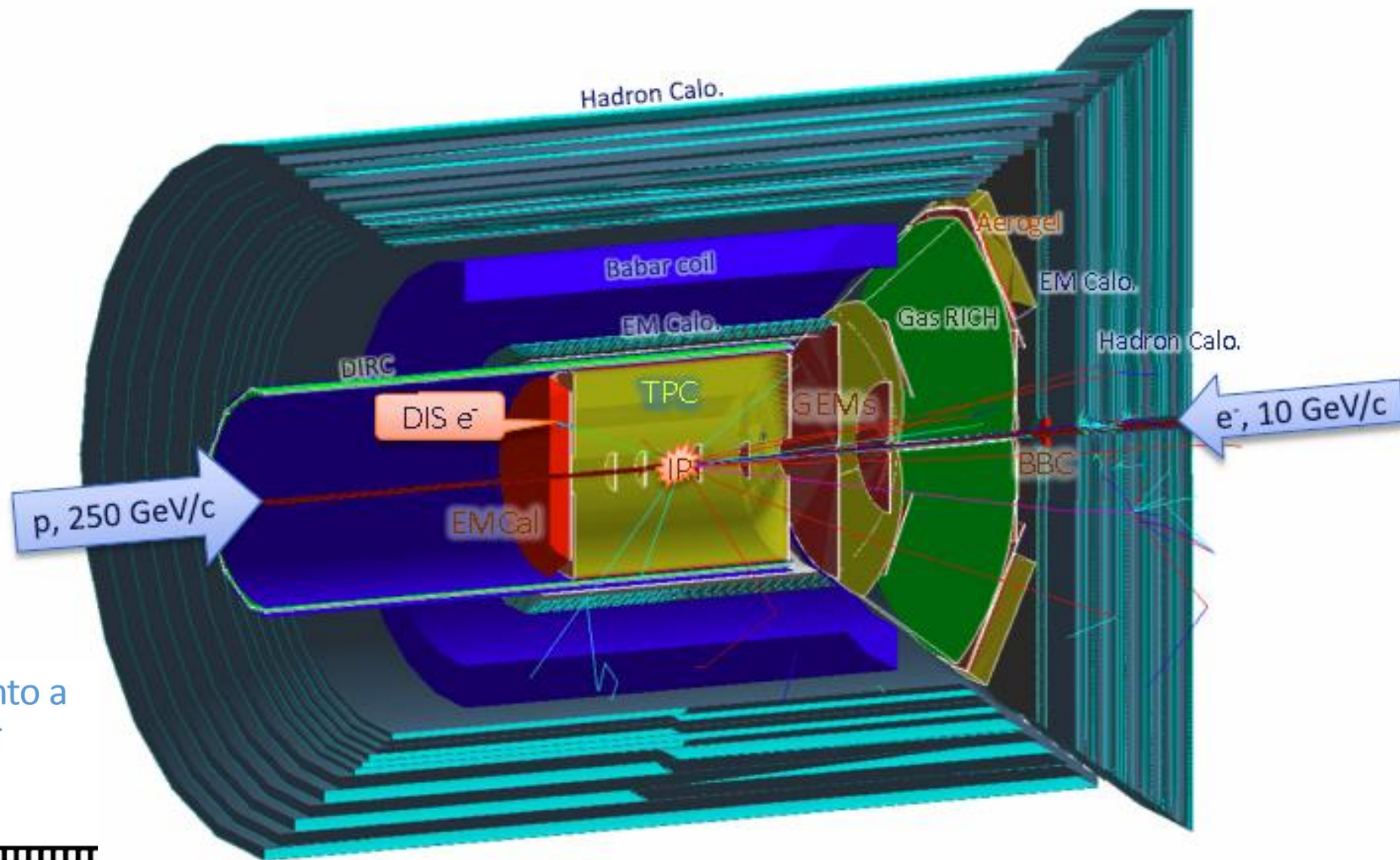


# Simulations

- DJANGO generator simulates DIS processes including QED and QCD radiation
  - ✓ Developed by Hubert Spiesberger and used at BNL for the EIC Charged Current study
- Electron-proton collisions to study new structure functions
  - ✓ The data is binned in  $(x, Q^2)$  two dimensions
  - ✓ Doing  $Y$  dependent fit to extract projections on  $F_1^{YZ}$ ,  $F_3^{YZ}$ ,  $g_1^{YZ}$ ,  $g_5^{YZ}$
- $\sin^2\Theta_w$  projections are from electron beam asymmetries in e-D collisions
- Highlights of the study:
  - ✓ Cuts:
    - ❑  $Q^2 > 1 \text{ GeV}^2$ ,  $W_h > 2 \text{ GeV}$ ,  $y > 0.1$ ,  $p$  cut for structure function studies
    - ❑  $Q^2 < 6400 \text{ GeV}^2$  and  $x > 0.2$  in addition for  $\sin^2\Theta_w$  studies
  - ✓ Unfolding for kinematical migration due to radiation and finite detector resolution



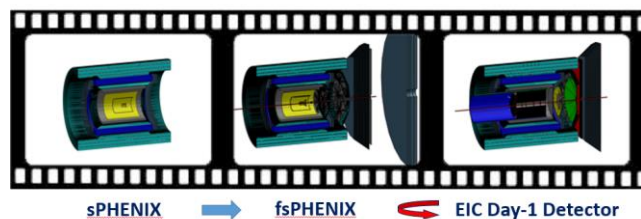
# ePHENIX



Evolution of PHENIX into a  
Day-1 EIC Detector


Kenneth N. Barish  
UC Riverside


Please refer to ePHENIX LOI for the details



# Detector resolutions for inclusive electrons

sPHENIX		ePHENIX
	Barrel ( $-1.1 < \eta < 1.1$ )	electron going direction
Tracking	$\theta$ (mrad)	10
	$\phi$ (mrad)	0.3
EMCal:	$\frac{dp_T}{p_T}$	$0.65\% (+) 0.09\% * p_T$
	$\frac{dE}{E}$	$1\% (+) 2.5\% / \sqrt{E}$

  
Reference [2]

  
Reference [1]

Reference [1] ePHENIX letter of intent: <http://arxiv.org/abs/1402.1209>

Reference [2] sPHENIX pre-CDR design report: <https://indico.bnl.gov/conferenceDisplay.py?confId=1483>



# Luminosity and polarization table

e-p collisions	10x100, 10x250, 15x100, 15x250
Integrated luminosity	500 fb <sup>-1</sup>
Proton (electron) beam polarization	70% (80%)

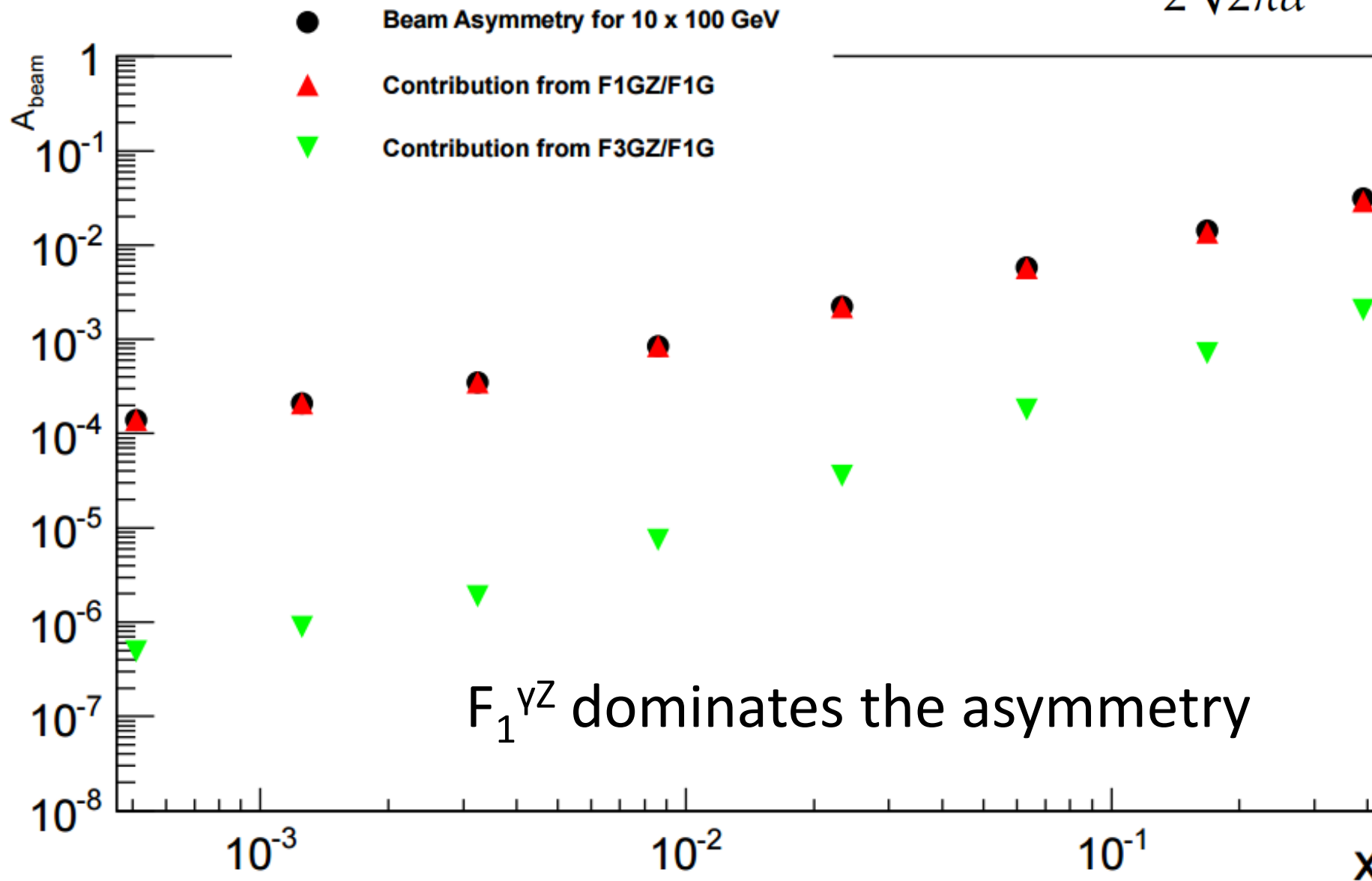
  

e-D collisions	10x50,10x125,15x50,15x125,20x125 GeV/u
Integrated luminosity	267 fb <sup>-1</sup>
Electron beam polarization	80%

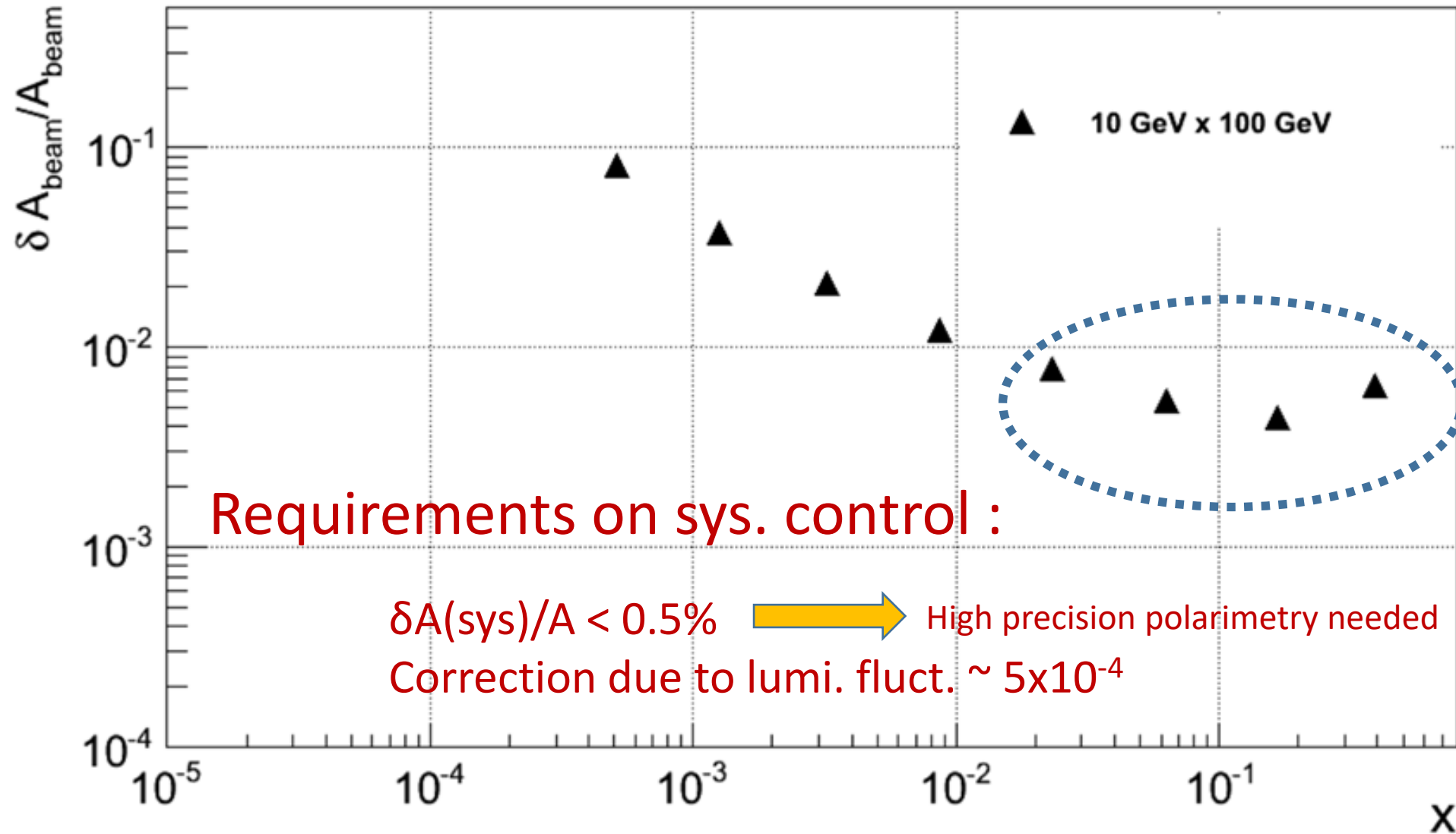
- **Unpolarized structure functions**
  - ❑ **e-p collisions**
  - ❑ **electron: longitudinally polarized**
  - ❑ **proton: unpolarized**
  - ❑ **Integrated luminosity: 500 fb<sup>-1</sup>**

# Predicted asymmetries

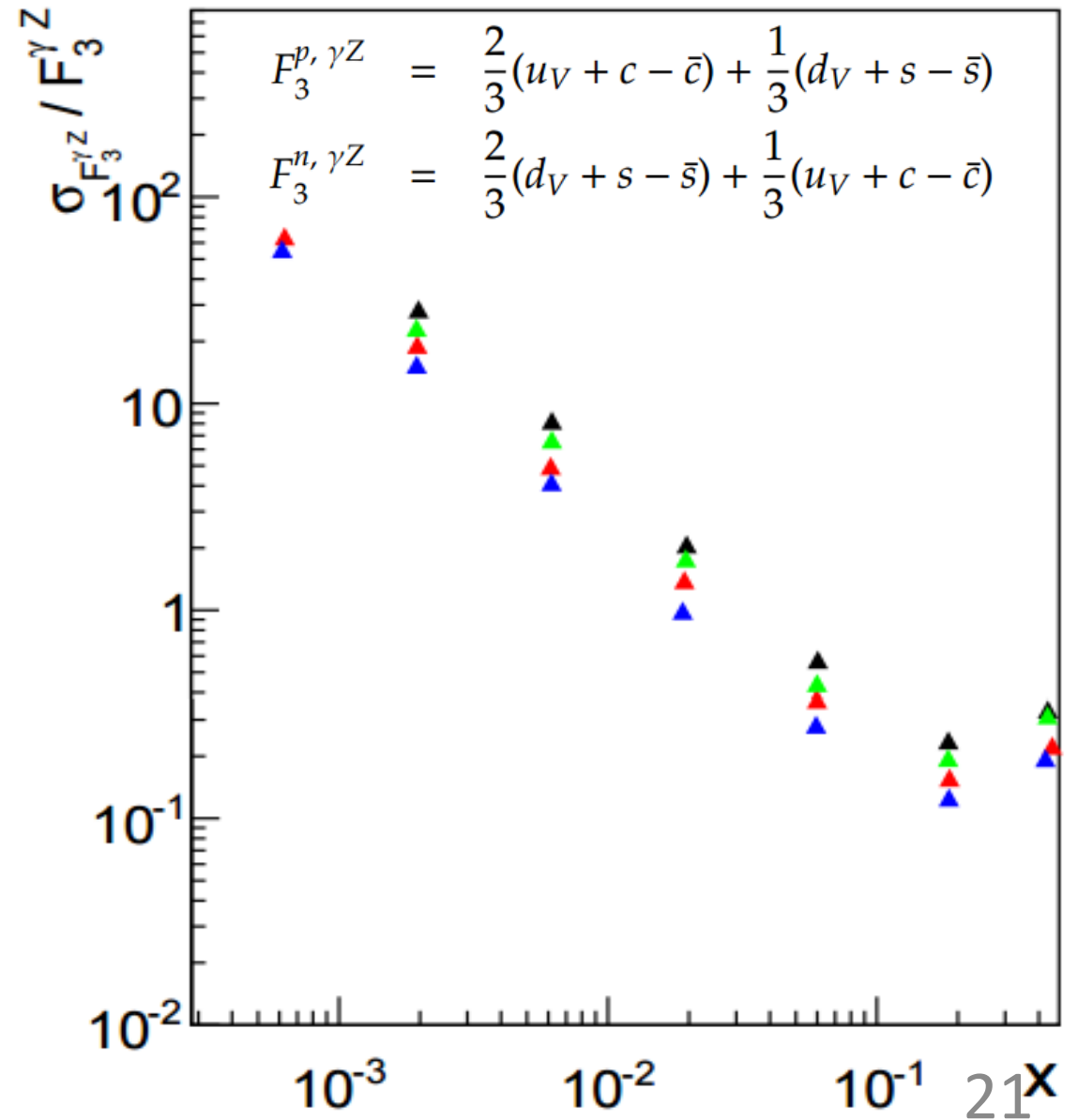
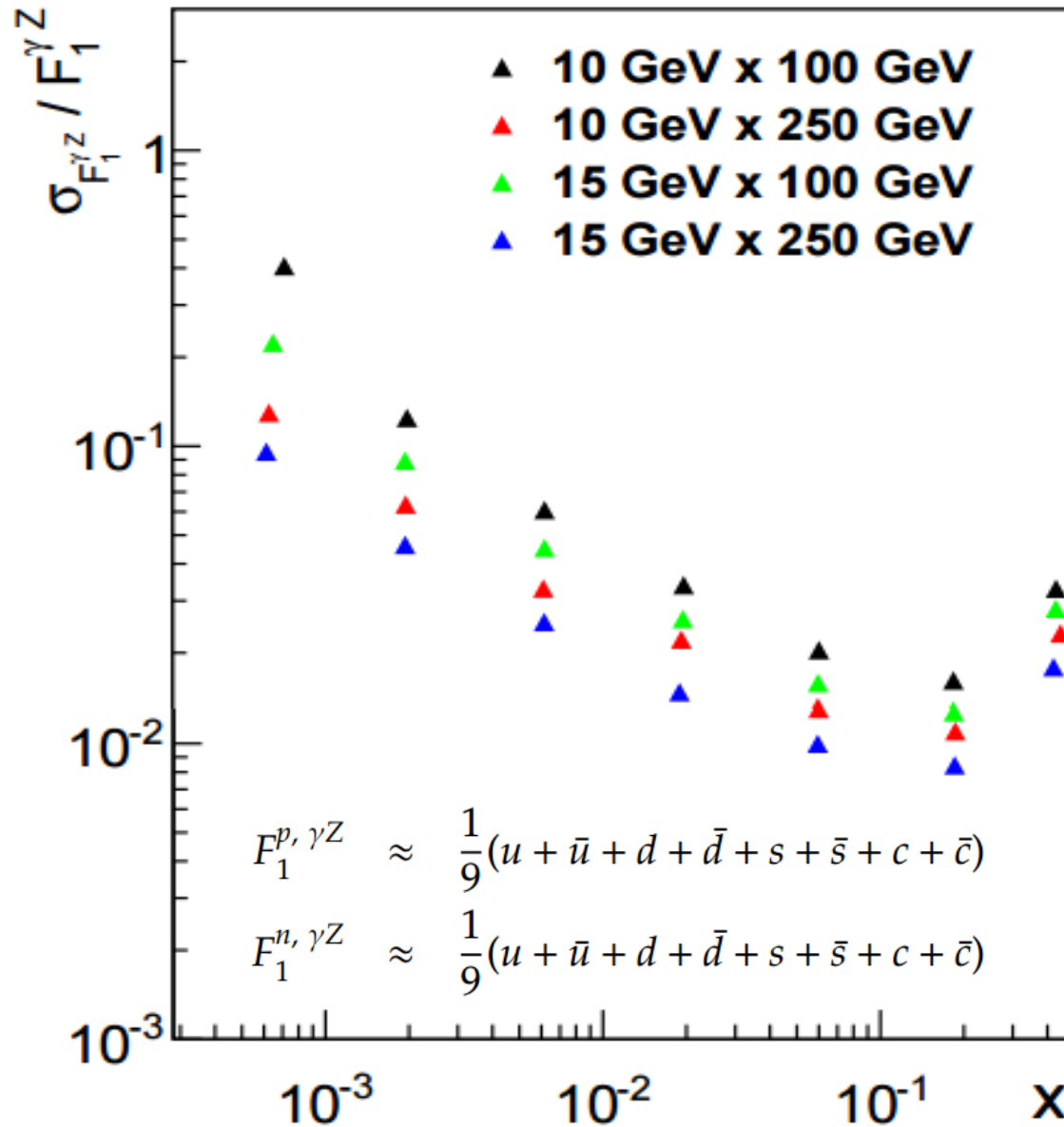
$$A_{beam} = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_A^e \frac{F_1^{\gamma Z}}{F_1^\gamma} + g_V^e \frac{\gamma_-}{2\gamma_+} \frac{F_3^{\gamma Z}}{F_1^\gamma} \right]$$



# $\delta A/A$ as a function of $x$



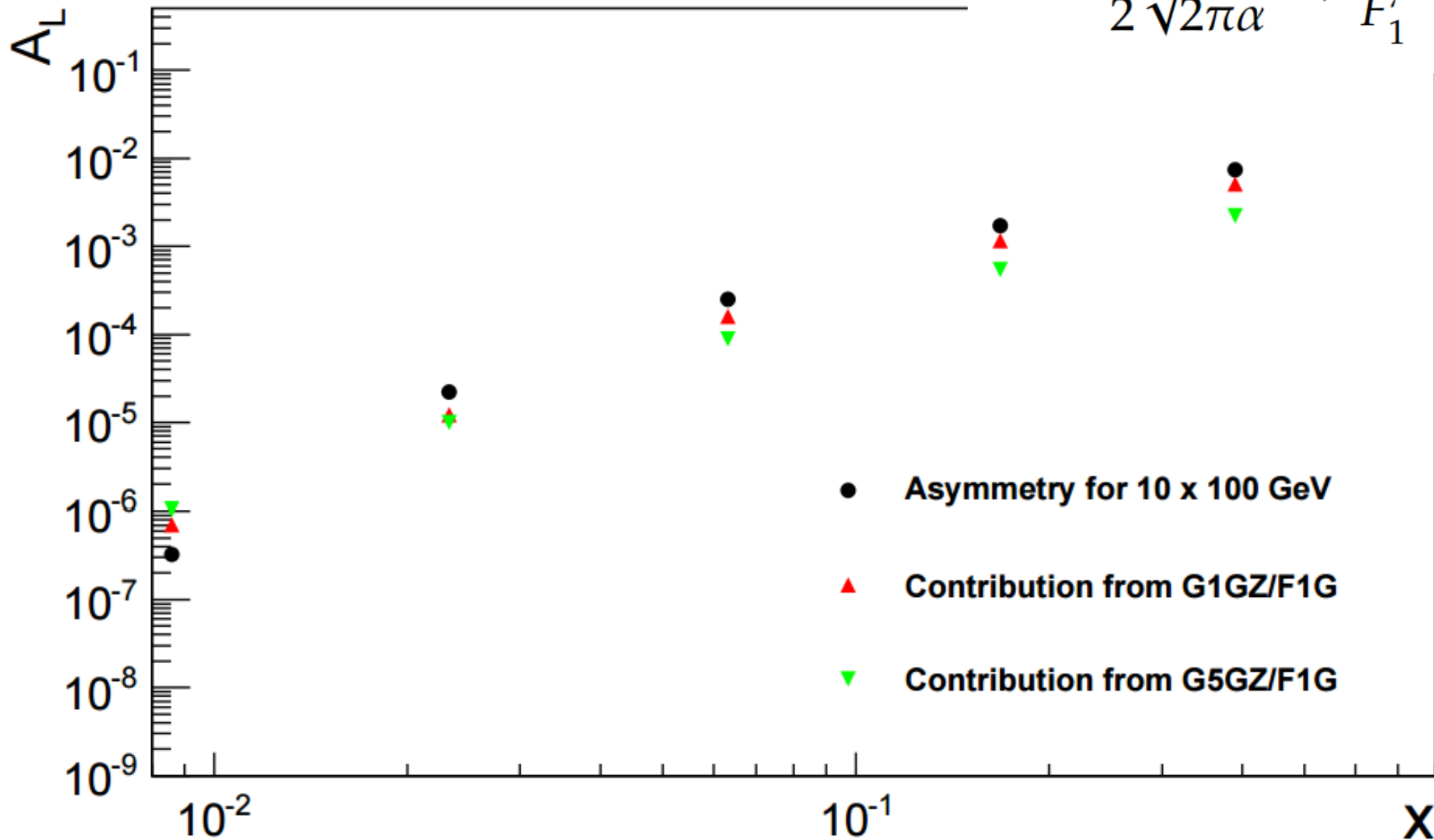
# Unpol. SFs projections after unfolding



- **Polarized structure functions**
  - ❑ **e-p collisions**
  - ❑ **e: unpolarized**
  - ❑ **p: longitudinally polarized**
  - ❑ **Integrated luminosity: 500 fb<sup>-1</sup>**

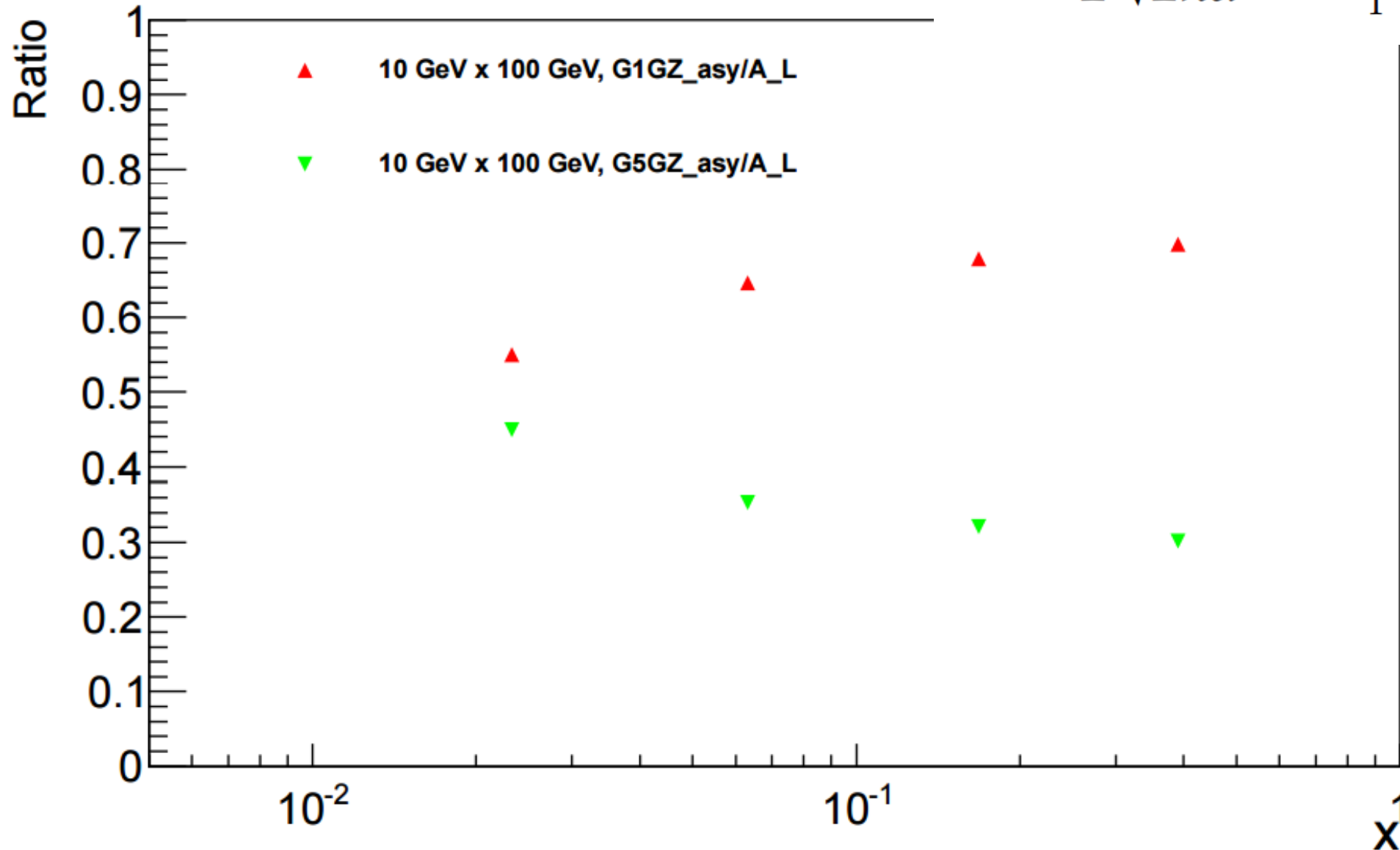
# Predicted asymmetries

$$A_L = \frac{G_F Q^2}{2 \sqrt{2} \pi \alpha} \left[ g_V^e \frac{g_5^{\gamma Z}}{F_1^{\gamma}} + g_A^e \frac{Y_-}{Y_+} \frac{g_1^{\gamma Z}}{F_1^{\gamma}} \right]$$



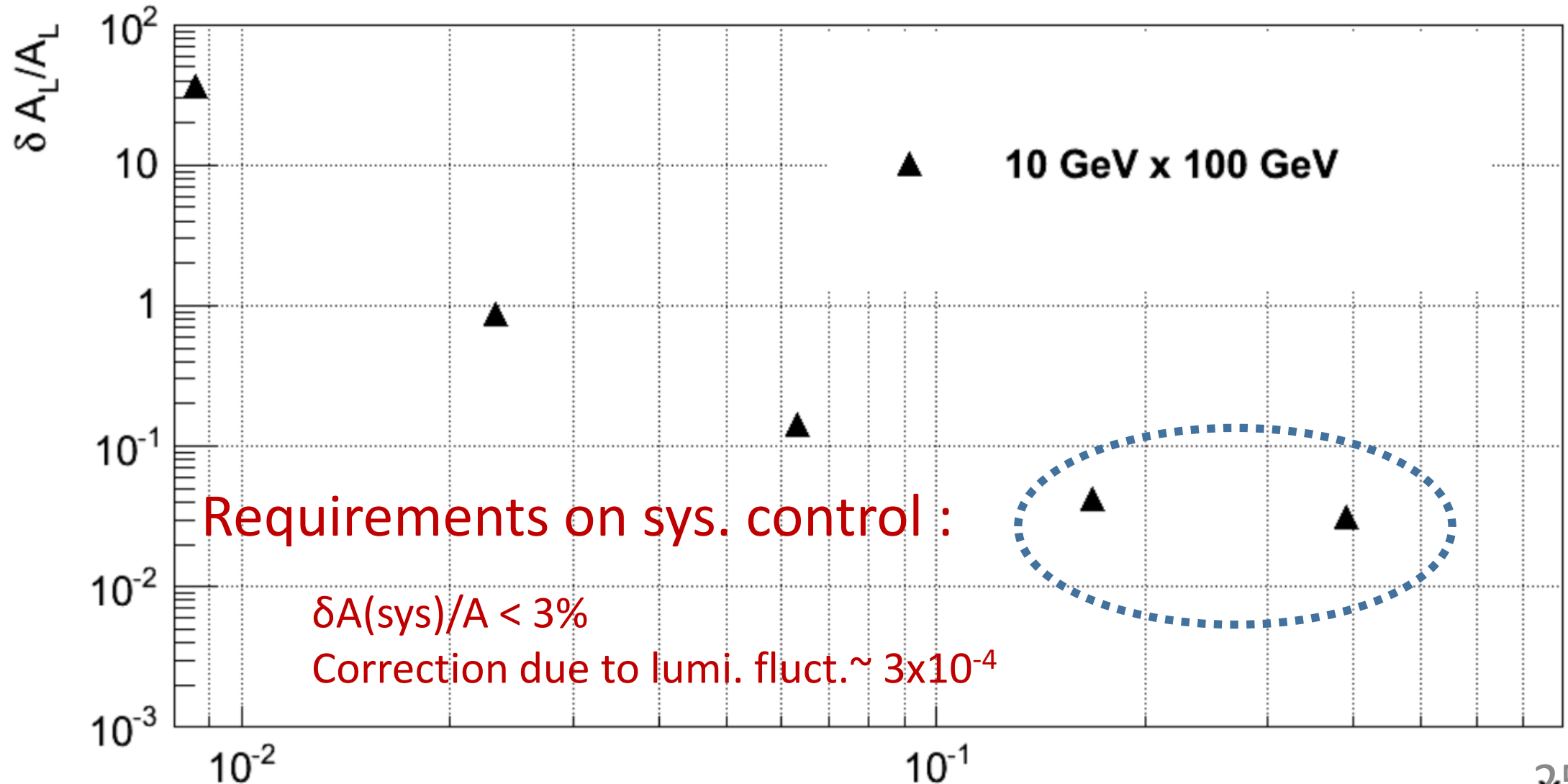
# Predicted asymmetries

$$A_L = \frac{G_F Q^2}{2 \sqrt{2} \pi \alpha} \left[ g_V^e \frac{g_5^{\gamma Z}}{F_1^{\gamma}} + g_A^e \frac{Y_-}{Y_+} \frac{g_1^{\gamma Z}}{F_1^{\gamma}} \right]$$

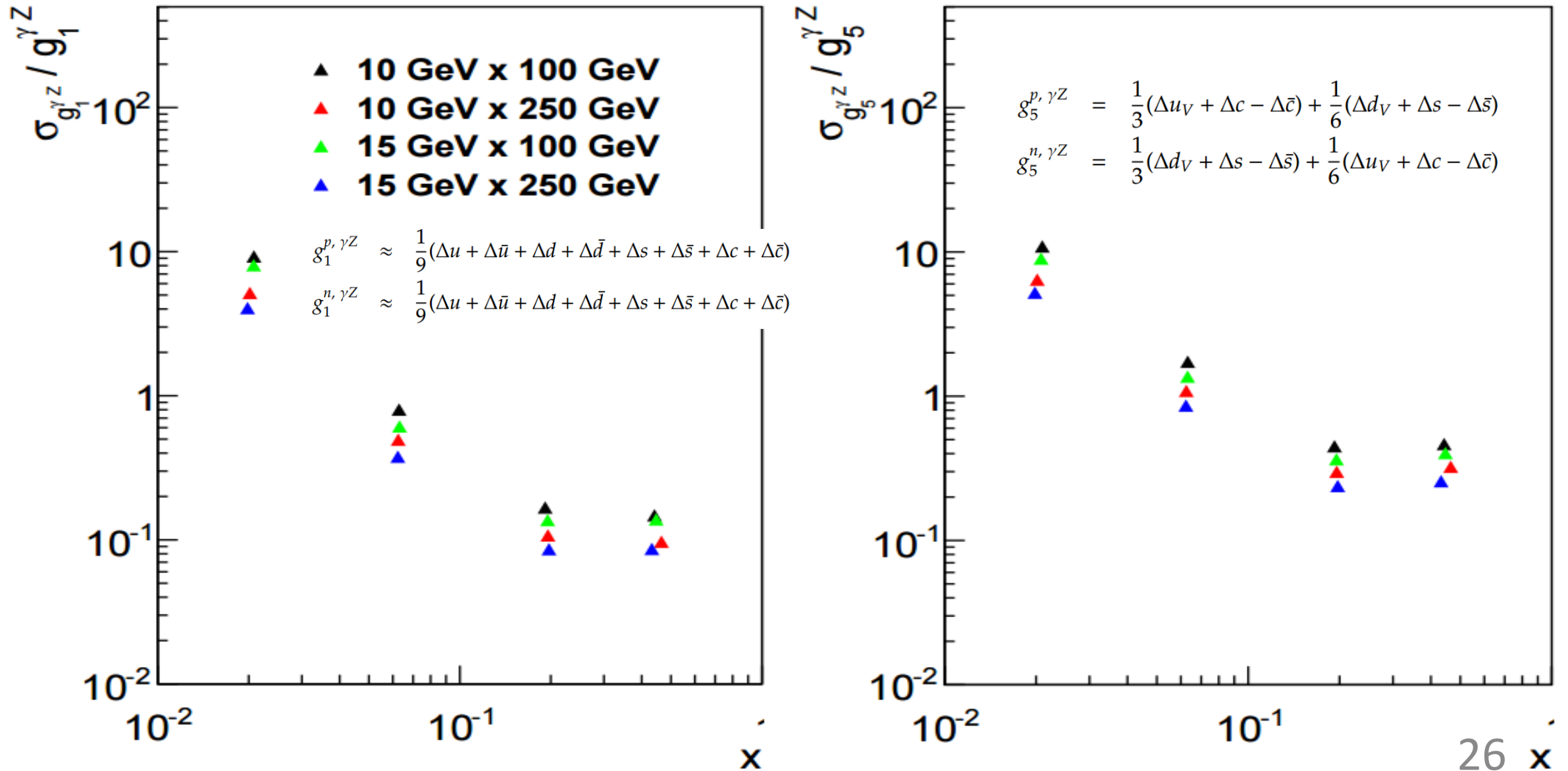




# $\delta A/A$ as a function of $x$

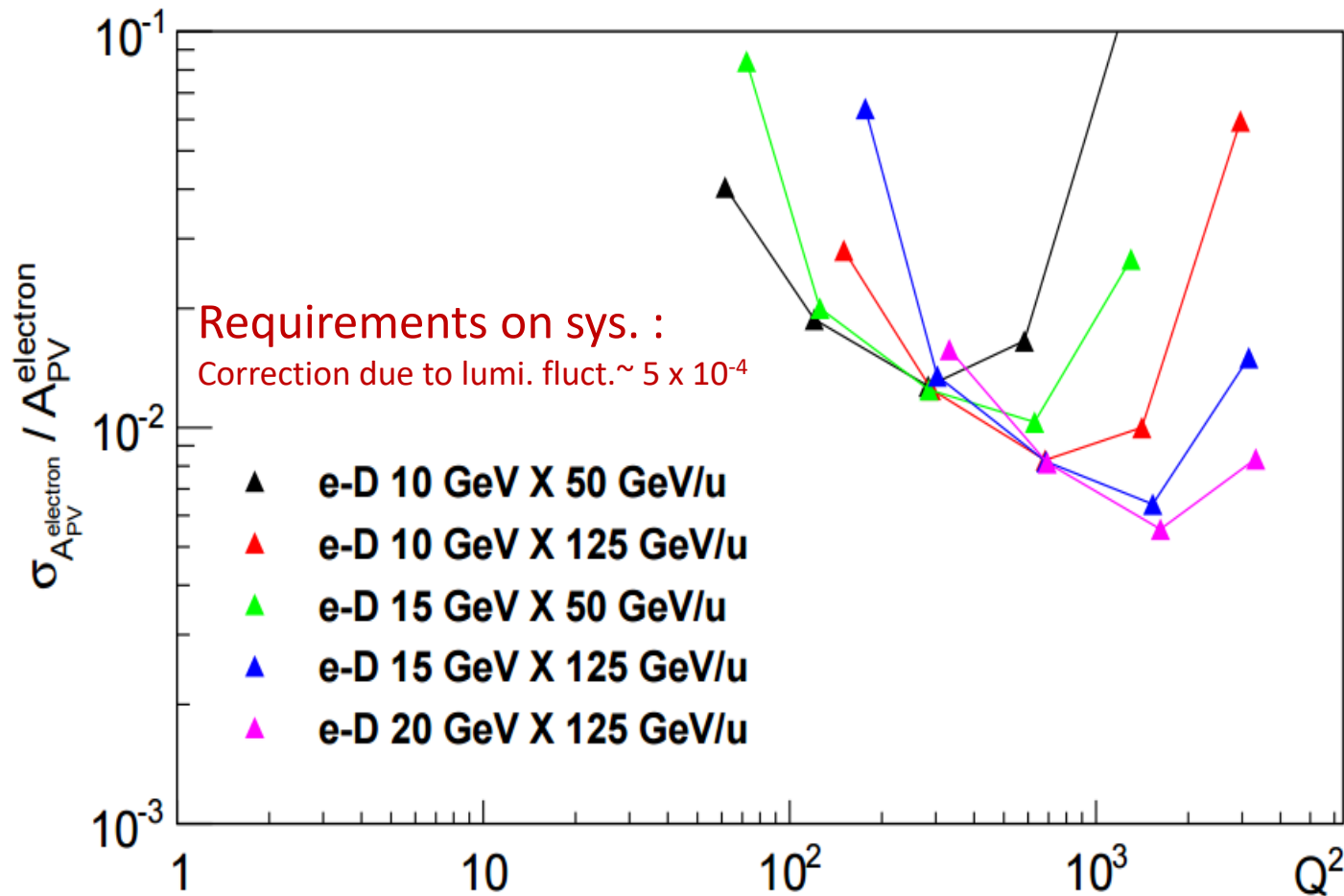


# Pol. SFs projections after unfolding



- **Weak mixing angle**
  - ❑ **e-D collisions**
  - ❑ **e: longitudinally polarized**
  - ❑ **D: unpolarized**
  - ❑ **Integrated luminosity: 267 fb<sup>-1</sup>**

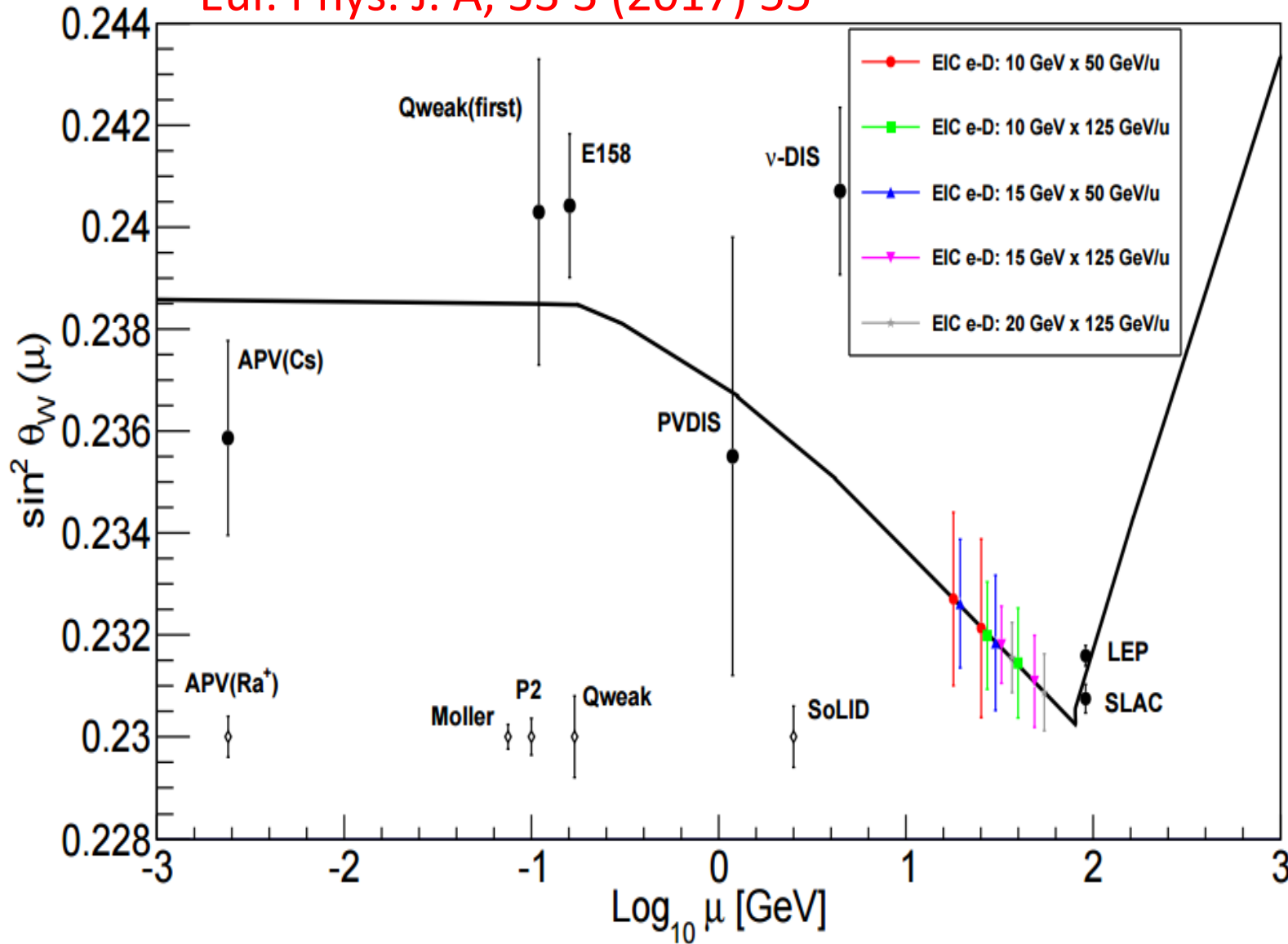
# $\delta A/A$ for e-D collisions



- A challenge for electron polarimetry
- Polarimetry  $\sim 1\%$  at the beginning and then 0.5% for higher energy and higher luminosity

# World data of $\sin^2\theta_w$ including EIC projections

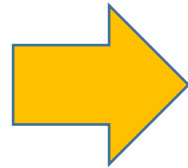
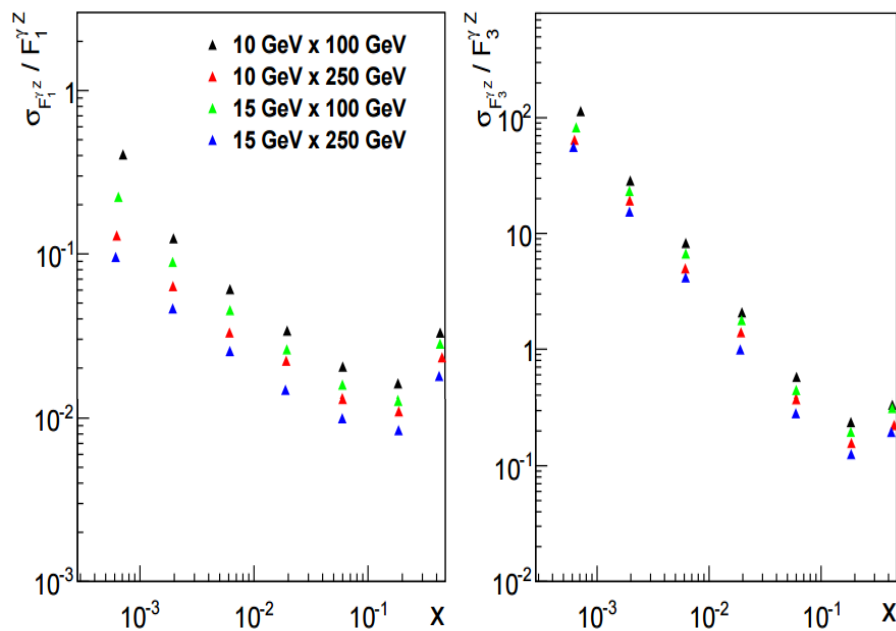
Eur. Phys. J. A, 53 3 (2017) 55



- Can reach similar precision to SoLID measurement
- Interesting  $Q^2$  region

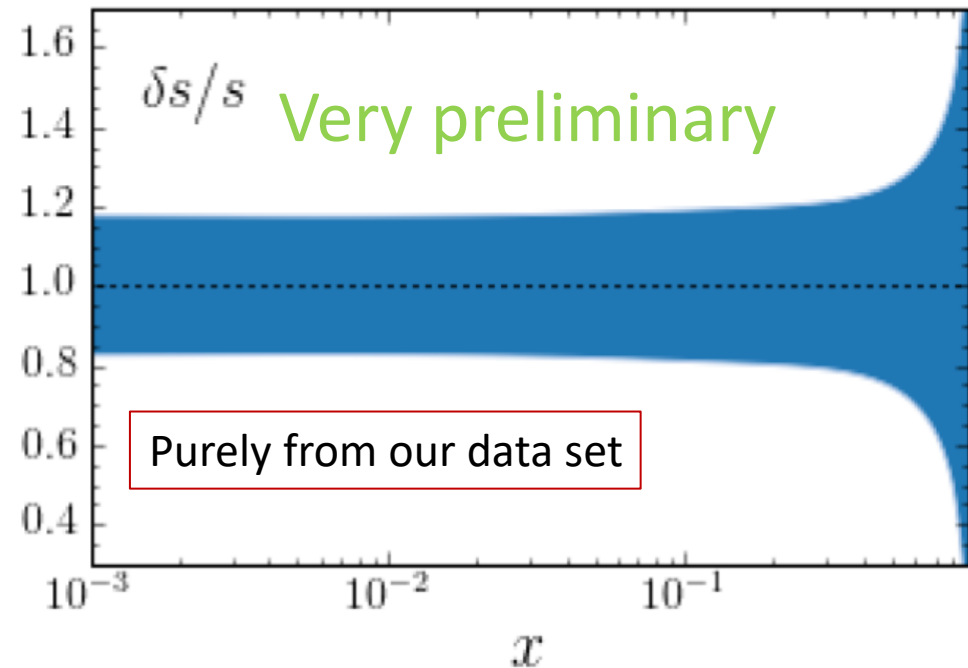
# Frist trial of unpolarized PDF fit

$$A_{beam} = \frac{G_F Q^2}{2\sqrt{2}\pi\alpha} \left[ g_A^e \frac{F_1^{\gamma Z}}{F_1^{\gamma}} + g_V^e \frac{Y_-}{2Y_+} \frac{F_3^{\gamma Z}}{F_1^{\gamma}} \right]$$



Alberto Accardi, etc.

— CJ15+EIC  
15x250 GeV<sup>2</sup>



To study the impact of these new structure functions → require fitting program to include electroweak physics

# Summary

- new unpolarized/polarized structure functions
  - ✓ Clean access to  $s$  and  $\Delta s$  PDFs
- weak mixing angle
  - ✓ Reach relative high precision in an interesting  $Q^2$  region
- Eur. Phys. J. A, 53 3 (2017) 55 for more details
- Detector requirements:
  - ✓  $<1\%$  polarimetry for electron beam
  - ✓  $<3\%$  polarimetry for proton beam

# Backups



# Center-of-mass table

Beam energy configuration (e x p, GeV )	Center of Mass ( GeV )
10 x 100	63
10 x 250	100
15 x 100	77
15 x 250	122
20 x 250	141